

The point values for each question is given within []. The total number of points for this assignment is 40.

- [2] 1. Consider the monoid $(\mathbb{Z}, +)$. Compute $\langle\{5\rangle\rangle$, the submonoid generated by the set $\{5\}$.
- [4] 2. Consider the grammar $\langle T, N, S, P \rangle$, where $T = \{+, *, (,), n\}$, $N = \{S\}$, $S = S$, and P is defined by

$$S \rightarrow S + S \mid S * S \mid (S) \mid n$$

Provide parse trees for the following strings:

- (a) $n * (n + n)$
- (b) $n * n + n$

- [4] 3. Consider the grammar $\langle T, N, S, P \rangle$, where $T = \{+, *, (,), n\}$, $N = \{E, T, F\}$, $S = E$, and P is defined by

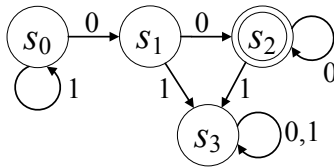
$$\begin{aligned} E &\rightarrow E + T \mid T \\ T &\rightarrow T * F \mid F \\ F &\rightarrow (E) \mid n \end{aligned}$$

Provide parse trees for the following strings:

- (a) $n * (n + n)$
- (b) $n * n + n$

- [5] 4. Consider the set of all bitstrings that begin and end with a 1.
 - (a) Provide a grammar for the language.
 - (b) Use your grammar to produce a parse tree for the string 10101

- [3] 5. Give a regular expression for the set recognized by the following finite automaton:



- [6] 6. Give a regular expression for set of bitstrings
 - (a) containing an even number of 0s
 - (b) that begin with a 0 and end with 010
- [3] 7. Provide a finite automaton that recognizes the set of bitstrings that begin with a 0 and end with 010.
- [5] 8. Find a context-free grammar that generates the language $L = \{s s^R \mid s \in \{0, 1\}^* \text{ and } s^R \text{ is the reverse of string } s\}$.
- [8] 9. Consider the regular expression $(1^*0(01)^*)|(00^*)$.
 - (a) Provide a context-free grammar $G = \langle T, N, S, P \rangle$ for strings represented by the regular expression.
 - (b) Given your G , draw a parse tree for 00000000.
 - (c) Given your G , draw a parse tree for 00101.
 - (d) Given your G , draw a parse tree for 1110.